Symmetric Achromatic Variability: A New and Totally Unexpected Phenomenon

> Anthony Readhead Caltech

### TeVPA - OSU August 10, 2017

Thursday, August 10, 17

Traditionally there have been two ways of detecting gravitational lensing:

1. Multiple Images

2. Time Delayed Variations

We believe there is now a third, until now totally unsuspected, way:

3. Symmetric Achromatic Variability That not only gives us a totally new approach to

gravitational lensing but, also provides microarcsecond resolution on some active galactic nuclei - i.e. a factor 30-100x better resolution than mm VLBI Symmetric Achromatic Variability in Active Galaxies -A Powerful New Gravitational Lensing Probe? arXiv:1702.06582

### The Peculiar Light Curve of J1415+1320 -A Case Study in Extreme Scattering Events arXiv:1702.05519

H. K. Vedantham<sup>1\*</sup>, A. C. S. Readhead<sup>1</sup>, T. Hovatta<sup>2,3,4</sup>,
T. J. Pearson<sup>1</sup>, R. D. Blandford<sup>5</sup>, M. A. Gurwell<sup>6</sup>,
A. Lähteenmäki<sup>2</sup>, W. Max-Moerbeck<sup>7</sup>, V. Pavlidou<sup>8</sup>,
V. Ravi<sup>1</sup>, R. A. Reeves<sup>9</sup>, J. L. Richards<sup>1</sup>,
M.Tornikoski<sup>2</sup>, J. A. Zensus<sup>6</sup>

To be published in ApJ next week (8/15/17)

Symmetric Achromatic Variability in Active Galaxies -A Powerful New Gravitational Lensing Probe? arXiv:1702.06582

> The Peculiar Light Curve of J1415+1320 -A Case Study in Extreme Scattering Events arXiv:1702.05519

#### Harish Vedantham

H. K. Vedantham<sup>1\*</sup>, A. C. S. Readhead<sup>1</sup>, T. Hovatta<sup>2,3,4</sup>,
T. J. Pearson<sup>1</sup>, R. D. Blandford<sup>5</sup>, M. A. Gurwell<sup>6</sup>,
A. Lähteenmäki<sup>2</sup>, W. Max-Moerbeck<sup>7</sup>, V. Pavlidou<sup>8</sup>,
V. Ravi<sup>1</sup>, R. A. Reeves<sup>9</sup>, J. L. Richards<sup>1</sup>,
M.Tornikoski<sup>2</sup>, J. A. Zensus<sup>6</sup>

To be published in ApJ next week (8/15/17)

Fermi-GST launch 11 June 2008

40 m Telescope 15 GHz monitoring program since 2008 in support of *Fermi*-GST: ~1830 objects twice a week. This program has amassed ~12,000 object-years on Active Galaxies and the OVRO data have been used in a paper per month in refereed journals for the last 8 years - now up to 95 papers using this data with no sign of a drop off





associated with the flux density variations.

Rees1966, Nature, 211, 468

APPEARANCE OF RELATIVISTICALLY EXPANDING RADIO SOURCES

Explained rapid variability in PEGRS
 Predicted superluminal motion

### The first unification paper

Rees 1967, MNRAS, 135,345



emitting regions which is >> the light-travel time associated with the flux density variations.

Rees1966, Nature, 211, 468

APPEARANCE OF RELATIVISTICALLY EXPANDING RADIO SOURCES

Explained rapid variability in PEGRS
 Predicted superluminal motion

### The first unification paper

Rees 1967, MNRAS, 135,345

STUDIES IN RADIO SOURCE STRUCTURE

Gubbay, Legg, Robertson, Moffet, Ekers, Seidel 1969 Nature 224, 1094 Moffet, Gubbay, Robertson & Legg 1972 IAUS, 44, 228 (conference was in 1970 - proceedings 2 years later)

Cohen et al. 1971, ApJ, 170, 207 Whitney et al. 1971, Science, 173, 225



associated with the flux density variations.

Rees1966, Nature, 211, 468

APPEARANCE OF RELATIVISTICALLY EXPANDING RADIO SOURCES

Explained rapid variability in PEGRS
 Predicted superluminal motion

### The first unification paper

Rees 1967, MNRAS, 135,345

STUDIES IN RADIO SOURCE STRUCTURE Gubbay, Legg, Robertson, Moffet, Ekers, Seidel 1969 Nature 224, 1094 Moffet, Gubbay, Robertson & Legg 1972 IAUS, 44, 228 (conference was in 1970 - proceedings 2 years later) Cohen et al. 1971, ApJ, 170, 207

Whitney et al. 1971, Science, 173, 225

Since AGN monitoring has been going on for 50 years it is surprising, to say the least, to find a strong signature that has not been noticed before, although it has been detected before but not recognized because it is masked by intrinsic variability

#### Calibrators



Thursday, August 10, 17

#### Strong Sources ( > 1 Jy)













#### Weaker Sources (0.1 Jy - 1 Jy)

J0017-0512









2008 2008.5 2009 2009.5 2010 2010.5 2011 2011.5 2012 2012.5 2013 2013.5 2014 2014.5 2015 2015.5 2016







#### Under-sampled



We have a sample of a dozen of such highly variable objects that we are monitoring on AMI

Thursday, August 10, 17

Flux Density [Jy]

Flux



Thursday, August 10, 17

Extreme Scattering Events (ESEs)



Fiedler, Dennison, Johnston & Hewish 1987 Nature 326, 625

Thursday, August 10, 17





ESEs are rare events: Fiedler et al. ApJ 1994, 430, 581 In 430 object-years of data 8 U-shaped dips were seen at 2695 MHz and 0 U-shaped dips were seen at 8085 MHz - so at high radio frequencies U-shaped dips are **VERY RARE!** 

1749+096

 $\sim$ 

С

0

С

0

0

87.5

88

Year

Flux Density (Jy)

2695 MHz

3250 MHz

4675 MHz

085 MH-

88.5

But we did see a small number of U-shaped events in our 12,000 objects hours of observing on the 40 m, but only one had been published until this month:

High and the second second

A. B. Pushkarev et al.: Refractive multiple imaging of the quasar 2023+335

Pushkarev et al 2013, A&A, 555, A80.

Thursday, August 10, 17

#### An Extreme Scattering Event in J1415+1320 (PKS 1413+135)?



#### An Extreme Scattering Event in J1415+1320 (PKS 1413+135)?



#### An Extreme Scattering Event in J1415+1320 (PKS 1413+135)?





It cannot be an ESE - it's highly achromatic from 15 GHz to 234 GHz

### The Peculiar Light Curve of J1415+1320 -A Case Study in Extreme Scattering Events arXiv:1702.05519

H. K. Vedantham<sup>1\*</sup>, A. C. S. Readhead<sup>1</sup>, T. Hovatta<sup>2,3,4</sup>,
T. J. Pearson<sup>1</sup>, R. D. Blandford<sup>5</sup>, M. A. Gurwell<sup>6</sup>,
A. Lähteenmäki<sup>2</sup>, W. Max-Moerbeck<sup>7</sup>, V. Pavlidou<sup>8</sup>,
V. Ravi<sup>1</sup>, R. A. Reeves<sup>9</sup>, J. L. Richards<sup>1</sup>,
M.Tornikoski<sup>2</sup>, J. A. Zensus<sup>6</sup>



radio source at z~0.5



edge-on Sa spiral galaxy at z = 0.247

OVRO 40 m Telescope









radio source at z~0.5



edge-on Sa spiral galaxy at z = 0.247 We believe that the SAV we are observing are due to lensing by  $\sim 10^3 - 10^4$  solar mass condensates in the edge-on Sa galaxy These condensates need to have a surface density integrated through the galaxy of  $10^4$  solar masses per square pc

> OVRO 40 m Telescope





radio source at z~0.5

As successive components are ejected along the jet they pass behind the intervening lens system moving at apparent speed ~c and repeatedly trace out a ~1-year flux density variation due to magnification by the lens



edge-on Sa spiral galaxy at z = 0.247 We believe that the SAV we are observing are due to lensing by  $\sim 10^3 - 10^4$  solar mass condensates in the edge-on Sa galaxy These condensates need to have a surface density integrated through the galaxy of  $10^4$  solar masses per square pc

40 m Telescope

**OVRO** 



There are currently two ways of detecting gravitational lensing:

1. multiple images

2. time delays between variations seen along the different lines of sight to the different images

radio source at z~0.5

As successive components are ejected along the jet they pass behind the intervening lens system moving at apparent speed ~c and repeatedly trace out a ~1-year flux density variation due to magnification by the lens



edge-on Sa spiral galaxy at z = 0.247 We believe that the SAV we are observing are due to lensing by  $\sim 10^3 - 10^4$  solar mass condensates in the edge-on Sa galaxy These condensates need to have a surface density integrated through the galaxy of  $10^4$  solar masses per square pc

> OVRO 40 m Telescope





radio source at z~0.5

As successive components are ejected along the jet they pass behind the intervening lens system moving at apparent speed ~c and repeatedly trace out a ~1-year flux density variation due to magnification by the lens

1. multiple images

the different images

edge-on Sa spiral galaxy at z = 0.247 We believe that the SAV we are observing are due to lensing by  $\sim 10^3 - 10^4$  solar mass condensates in the edge-on Sa galaxy These condensates need to have a surface density integrated through the galaxy of  $10^4$  solar masses per square pc

There are currently two ways of detecting gravitational lensing:

2. time delays between variations seen along the different lines of sight to

If SAV is due to gravitational lensing it will provide a third method for the detection of gravitational lensing as well as micro-arcsecond resolution of AGN - a factor 30 to 100 times better than is available now through mm VLBI, which could only be matched by mm VLBI from space OVRO 40 m Telescope



# Papers suggesting that some, or all, variability in AGN is due to gravitational lensing (refs in red specifically J1415+1320)

this is not an exhaustive list

Chang & Refsdal 1979 Nature, 282, 561 Narasimha, Subramanian & Chitre 1984 MNRAS, 210,79 Subramanian, Chitre & Narasimha, 1985 ApJ, 289, 37 Ostriker & Vietri 1985 Nature, 318, 446 & 1990 Nature 344,45 Schneider & Weiss 1987 A&A, 171, 49 Stickel et al. 1988 A&A, 198, L13 Gopal-Krishna & Subramanian 1991 Nature, 349, 766 Subramanian & Gopal-Krishna 1991 A&A, 248, 55 Carilli et al. 1992 ApJ, 400, L13 Stocke et al. 1992 ApJ, 400, L17 Perlman et al. 1994 ApJ, 424, L69 Gopal-Krishna & Subramanian 1996 A&A, 315, 343 Webb et al. 2000 AJ, 120, 41

# Papers suggesting that some, or all, variability in AGN is due to gravitational lensing (refs in red specifically J1415+1320)

this is not an exhaustive list

Chang & Refsdal 1979 Nature, 282, 561 Narasimha, Subramanian & Chitre 1984 MNRAS, 210,79 Subramanian, Chitre & Narasimha, 1985 ApJ, 289, 37 Ostriker & Vietri 1985 Nature, 318, 446 & 1990 Nature 344,45 Schneider & Weiss 1987 A&A, 171, 49 Stickel et al. 1988 A&A, 198, L13 Gopal-Krishna & Subramanian 1991 Nature, 349, 766 Subramanian & Gopal-Krishna 1991 A&A, 248, 55 Carilli et al. 1992 ApJ, 400, L13 Stocke et al. 1992 ApJ, 400, L17 Perlman et al. 1994 ApJ, 424, L69 Gopal-Krishna & Subramanian 1996 A&A, 315, 343 Webb et al. 2000 AJ, 120, 41

These papers suggested that J1415+1320 is a background source because:

 this is a BL Lac object and these are very rarely, if ever, associated with spiral galaxies
 it has an extremely red spectrum, presumably due to high extinction in foreground Sa galaxy
 if an AGN were buried in the Sa galaxy it would heat the copious dust and gas around the nucleus and we would see a bright mid infra-red point source and bright narrow line emission, which are not seen

Thursday, August 10, 17



It appears that we've been somewhat lucky (or unlucky if nature is just teasing us) and that the reasons that we've been able to pick out the SAV in J1415+1320 are:

1. the high sensitivity and

2. high cadence, of our 40 m Telescope observations, combined with

3. the relatively low level of intrinsic activity in the object between 2008 and 2016

## 1158 objects in complete sample 981 of them of sufficient quality to look for U-features:

two independent searches - 10 features (in 7 objects)  $\sim 1\%$  probability of seeing a feature in any object in 8 years.

We see three more features in J1415+1320 over 27 years (probability =  $4x10^{-3}$ ) and we see three features in J0310+3014 over 8 years (probability =  $10^{-3}$ )

Unless nature is teasing us it seems highly unlikely that these are just random juxtapositions of two "flares"



### Could these features be due to a pair of forward-reverse shocks, such as those modeled in GRBs?

The symmetry is then hard to explain (see e.g. Kobayashi & Zhang 2003 ApJ, 582, L75)



FIG. 1.—Optical light curve: Modeling with p = 2.4, forward shock emission (*dash-dotted line*), reverse shock emission (*dashed line*), total flux (*thick solid line*), and accurate spectrum mode (*dotted line*),  $\epsilon_B = 3.0 \times 10^{-3}$ ,  $\epsilon_e = 0.28$ . n = 0.45 protons cm<sup>-3</sup>,  $\eta = 120$ , and  $E = 5.6 \times 10^{52}$  ergs. Modeling with p = 2.2 and total flux (*thin solid line*),  $\epsilon_B = 3.0 \times 10^{-3}$ ,  $\epsilon_e = 0.32$ . n = 0.45 protons cm<sup>-3</sup>,  $\eta = 140$ , and  $E = 5.6 \times 10^{52}$  ergs. Measurements are shown as circles, and upper limits as triangles. Data are from Bersier et al. 2002b; Fox 2002; Halpern et al. 2002a, 2002b; Holland et al. 2002a, 2002b; Malesani et al. 2002a, 2002b; Masetti et al. 2002; Masumoto et al. 2002a, 2002b; Mirabal et al. 2002a, 2002b; Oksanen & Aho 2002; Oksanen et al. 2002; Stanek et al. 2002; Stefanon et al. 2002; Torii et al. 2002; Uemura et al. 2002; Weidinger et al. 2002; Winn et al. 2002; and Zharikov et al. 2002, following the calibration of Henden 2002.



FIG. 2.—Radio light curve: Modeling with p = 2.4, forward shock emission (*dash-dotted line*), reverse shock emission (*dashed line*), self-absorption limit (*dotted line*), and total flux (*thick solid line*). Modeling with p = 2.2 and total flux (*thin solid line*). The parameters are the same as in Fig. 1. Measurements are shown as circles with error bars and as an asterisk, and the upper limit as a triangle. Data are from Frail & Berger 2002; Pooley 2002a, 2002b, 2002c; and Berger et al. 2002.



FIG. 2. Influence of noncircular perturbations. (a) Image plane. A circular lens will produce a critical circle (solid line) radius  $r_o$ . When a noncircular perturbation is applied, in this case proportional to  $\cos 2\phi$ , the critical circle is deformed into an ellipse (dashed line). (b) Source plane. The perturbation modifies the caustic from a degenerate point at O to a curve  $c(\phi)$ , in this case a four-cusped asteroid.

Blandford & Kovner 1988 Phys. Rev., 38, 4028









Fast Rise-Slow Decline followed by Slow Rise-Fast Decline FRSD-SRFD: "Crater Symmetry"





Fast Rise-Slow Decline followed by Slow Rise-Fast Decline FRSD-SRFD: "Crater Symmetry"

p = 0.005

p = 0.01

p = 0.02



Slow Rise-Fast Decline followed by Fast Rise-Slow Decline SRFD-FRSD: "Volcano Symmetry" p = 0.005p = 0.01p = 0.02



![](_page_39_Figure_0.jpeg)

Blandford & Kovner 1988 Phys. Rev., 38, 4028

![](_page_40_Figure_2.jpeg)

FIG. 2. Influence of noncircular perturbations. (a) Image plane. A circular lens will produce a critical circle (solid line) radius  $r_o$ . When a noncircular perturbation is applied, in this case proportional to  $\cos 2\phi$ , the critical circle is deformed into an ellipse (dashed line). (b) Source plane. The perturbation modifies the caustic from a degenerate point at O to a curve  $c(\phi)$ , in this case a four-cusped asteroid.

Blandford & Kovner 1988 Phys. Rev., 38, 4028

![](_page_41_Figure_2.jpeg)

FIG. 2. Influence of noncircular perturbations. (a) Image plane. A circular lens will produce a critical circle (solid line) radius  $r_o$ . When a noncircular perturbation is applied, in this case proportional to  $\cos 2\phi$ , the critical circle is deformed into an ellipse (dashed line). (b) Source plane. The perturbation modifies the caustic from a degenerate point at O to a curve  $c(\phi)$ , in this case a four-cusped asteroid.

But this is a very simple gravitational potential perturbation! What happens if we're looking through a galaxy and there are several condensations along the line of sight? (they don't have to be gravitationally bound)

#### e.g. if there are two condensations and we add the underlying potential of the galaxy

![](_page_42_Figure_1.jpeg)

Note that the binary mass ratio is q = 0.01 so that we only need one mass condensation of  $10^3 - 10^4$  solar masses in the spiral and another mass of  $10^1 - 10^2$  solar masses *anywhere along the line of sight through the disc of the spiral galaxy* to produce such a binary gravitational lens i.e. once you have a single  $10^3 - 10^4$  solar mass condensate along the line of sight through the galaxy then any e.g. stellar masses greater than about 10 solar masses

along the line of sight through the galaxy will turn it into a caustic network

Thursday, August 10, 17

The Einstein radius is:

$$\theta_{\rm E} = (4GM/c^2D)^{1/2}$$
  
  $\approx 90 \, (M/10^3 \, M_{\odot})^{1/2} (D/1 \, {\rm Gpc})^{-1/2} \, \mu {\rm as}.$ 

Which for a high redshift (z~1) object  $\sim 100(v_{\perp}/c)(t/1{
m yr}) \ \mu{
m as}$ 

It is important to note that it is the **combination** of the lensing **mass** (here  $\sim 10^3 - 10^4$  solar masses), which produces a milli-lens with Einstein radius around 100 µarcsec, and the **distance** and **speed** of the background component, which are  $z\sim1$  and  $v\simc$ , that **together** give rise to a variation that can be seen on a timescale of a few months to a few years, and hence the whole lensing pattern can be observed before the component fades, as would happen if the background component were moving at the usual peculiar velocities we see in galaxies.

![](_page_44_Figure_0.jpeg)

![](_page_44_Figure_1.jpeg)

At this stage all one can say is that the fits to the high sensitivityhigh cadence 15 GHz data are very good, whereas the fits to the more noisy 37 GHz and less frequently sampled 234 GHz data are not implausible

![](_page_45_Figure_0.jpeg)

Figure S6: Multifrequency model light curves over plotted on data at 15, 37, and 234 GHz.

Curious things do happen and we are very good at picking out patterns where none actually exist (e.g. stellar constellations). BUT in this case, and unbeknownst to us --- for entirely different reasons, people have been suggesting for 25 years that J1415+1320 is a lensed object! Perlman et al. 2002 AJ, 124, 2401

The offset in position is 13 milliarcseconds, i.e. ~50 pc ---the probability is only .006, or one in 170, of such an alignment after taking into account the magnification How concerned should we be given that this is *a posteriori* statistics?

![](_page_46_Figure_2.jpeg)

![](_page_47_Figure_0.jpeg)

![](_page_48_Figure_0.jpeg)

### Note that the high frequency variations appear to precede the low frequency variations

#### For decades with VLBI we've been observing flat-spectrum cores at one end of steep-spectrum jets:

this + superluminal motion + the highly curved structures strongly suggested relativistic beaming of a jet pointed almost directly at us and as you observe at higher frequencies you drill down deeper into the jet

But does this always apply and does it apply at all energies? What about the gamma-ray emission?

3C 273

3C 345

![](_page_49_Figure_5.jpeg)

Readhead, Cohen, Pearson & Wilkinson 1978, Nature, 276, 768

Thursday, August 10, 17

At first we saw nothing to contradict this model in the observations, and when the CGRO EGRET observations at  $\gamma$ -ray energies came along it seemed highly probable in view both of their energy and very rapid variability that they are coming from even closer to the central engine

![](_page_50_Figure_1.jpeg)

FIG. 6.—Schematic representation of the pair cascade model. A relativistic jet is formed parallel to the spin of a massive black hole orbited by a thick accretion disk. Soft X-ray photons denoted SX emitted near the black hole may be Thomson-scattered into the jet. There they can both combine with  $\gamma$ -rays to form electrons and positrons and be inverse Compton scattered by electrons and positrons to form  $\gamma$ -rays. In this way a pair cascade can develop. Also shown are the  $\gamma$ -spheres for  $E_{\gamma} = 0.1, 1, 10$  GeV.

Jorstad, Marscher, et al. Ap.J. 556, 738, 2001

![](_page_51_Figure_2.jpeg)

![](_page_51_Figure_3.jpeg)

Quote from Abstract: "Our analysis . . . suggests that the  $\gamma$ -ray events occur in the superluminal radio knots. This implies that the  $\gamma$ -ray flares are caused by inverse Compton scattering by relativistic electrons in the parsec-scale regions of the jet rather than closer to the central engine."

**Fig. 1** Rough sketch of the structure and emission regions of a radio-loud active galaxy with a relativistic jet. Note the logarithmic scale on the bottom for the distance down the jet. In the two emission panels— one for jets viewed almost end-on (a blazar) and the other for those seen at a wider angle (a typical radio galaxy)—the likely waveband of photons that can be emitted at each site is indicated. If the jet accelerates out to parsec scales, the inner jet between the mm-wave core and the black hole may be essentially invisible in blazars, while in radio galaxies bright emission might extend down to the base of the jet. (Adapted from Marscher 2005.)

![](_page_52_Picture_0.jpeg)

![](_page_52_Picture_1.jpeg)

### Detection of significant cm to sub-mm band radio and $\gamma$ -ray correlated variability in *Fermi* bright blazars

L. Fuhrmann,<sup>1\*</sup> S. Larsson,<sup>2</sup> J. Chiang,<sup>3</sup> E. Angelakis,<sup>1</sup> J. A. Zensus,<sup>1</sup> I. Nestoras,<sup>1</sup> T. P. Krichbaum,<sup>1</sup> H. Ungerechts,<sup>4</sup> A. Sievers,<sup>4</sup> V. Pavlidou,<sup>1</sup> A. C. S. Readhead,<sup>5</sup> W. Max-Moerbeck<sup>5</sup> and T. J. Pearson<sup>5</sup>

![](_page_52_Figure_4.jpeg)

Thursday, August 10, 17

Conclusions:

1. If our gravitational lensing hypothesis for SAV behavior is confirmed, and furthermore if these objects are not anomalous, they could have profound implications for our interpretation of the relationship between the high-frequency and the low-frequency emission regions observed in AG jets.

2. The observed behavior is readily interpretable if the moving features are outwardly propagating particle acceleration/magnetic amplification fronts - i.e. shocks if the jet is plasma-dominated. The optically emitting electrons would cool close to the front and the centroid of their emission would cross any caustic ahead of the radio emission

3. Symmetric Achromatic provides a third observational approach to gravitational lensing and also provides micro-arcsecond resolution on the nuclei of some active galaxies.

Thursday, August 10, 17

![](_page_55_Figure_0.jpeg)

 $2008 \ 2008.5 \ 2009 \ 2009.5 \ 2010 \ 2010.5 \ 2011 \ 2011.5 \ 2012 \ 2012.5 \ 2013 \ 2013.5$ 2014 2014.5 2015 2015.5 2016

![](_page_56_Figure_0.jpeg)

Thursday, August 10, 17

![](_page_57_Figure_0.jpeg)

![](_page_57_Figure_1.jpeg)

![](_page_57_Figure_2.jpeg)

![](_page_58_Figure_0.jpeg)

![](_page_58_Figure_1.jpeg)

 $2008\ 2008.5\ 2009\ 2009.5\ 2010\ 2010.5\ 2011\ 2011.5\ 2012\ 2012.5\ 2013\ 2013.5\ 2014\ 2014.5\ 2015\ 2015.5\ 2016$ J1415 + 13201.61.4 Flux Density [Jy] 1.21.00.8 0.60.4 $(t_b+t_c)/2=1519.1+/-2.1$ 0.20.01000 1500 2000 50025000 Days since MJD 54466 (2008 Jan 1)

![](_page_59_Figure_0.jpeg)

![](_page_59_Figure_1.jpeg)

 $2008\ 2008.5\ 2009\ 2009.5\ 2010\ 2010.5\ 2011\ 2011.5\ 2012\ 2012.5\ 2013\ 2013.5\ 2014\ 2014.5\ 2015\ 2015.5\ 2016$ J1415 + 13201.61.4 Flux Density [Jy] 1.21.00.8 0.60.4 $(t_b+t_c)/2=1519.1+/-2.1$ 0.20.01000 1500 2000 50025000 Days since MJD 54466 (2008 Jan 1)